

# Lyapunov Functions for Random One-Sided Systems in Terms of Nonuniform Exponential Stability

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## 1 Abstract

In this study, we investigate the nonuniform exponential stability for a continuous linear random one-sided system. We derive necessary and sufficient conditions for this concept. As an extension for this study we establish Lyapunov type characterizations using Lyapunov functions. Additionally, we illustrate the essential properties that are derived in this directions for the adjoint and inverse systems associated for the original linear random one-sided system.

## References

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